



Facts and Reminders

Improper Fractions

An *improper fraction* always has a numerator equal to or greater than the denominator. The examples below are all improper fractions.

$$\frac{3}{2}$$

$$\frac{9}{9}$$

$$\frac{11}{10}$$

$$\frac{15}{3}$$

$$\frac{15}{3}$$
 $\frac{22}{12}$ $\frac{12}{9}$

$$\frac{12}{9}$$

Improper fractions are always equal to or greater than one. An improper fraction always means one or more than one whole object. It is one pizza or more than one pizza. It is one complete bag of candy or more than one complete bag.





$$=\frac{3}{2}$$



$$=\frac{1}{1}$$

Mixed Numbers

A mixed number contains a whole number and a fraction. It is always greater than one. For example, it might be one whole pizza and part of another. A mixed number might indicate three whole pies and part of another pie. Look at the examples below.









Here are more mixed numbers.

$$1\frac{1}{3}$$

$$2\frac{2}{5}$$

$$7\frac{1}{2}$$

$$1\frac{1}{3}$$
 $2\frac{2}{5}$ $7\frac{1}{2}$ $3\frac{1}{4}$ $4\frac{2}{7}$ $8\frac{1}{6}$

$$4\frac{2}{7}$$

$$3\frac{1}{6}$$

Changing Improper Fractions to Mixed Numbers or Whole Numbers

An improper fraction can be reduced to a whole number or a mixed number by dividing the denominator into the numerator. The quotient can be written as a whole number and the remainder, if there is one, as a fraction. Look at the example below.

$$\begin{array}{cc} \text{(numerator)} & \frac{7}{3} \\ \text{(denominator)} & \frac{7}{3} \end{array}$$

$$\frac{2}{3\sqrt{7}}$$
 R1 (quotient)

$$\frac{7}{3} = 2\frac{1}{3}$$

Here are more examples.

$$\frac{3}{2} = 1\frac{1}{2}$$
 $\frac{7}{5} = 1\frac{2}{5}$ $\frac{12}{4} = 3$

$$\frac{7}{5} = 1\frac{2}{5}$$

$$\frac{12}{4} = 3$$

The mixed number $1\frac{1}{2}$ and the improper fraction $\frac{3}{2}$ both indicate the same amount. The mixed number $1\frac{2}{5}$ and the improper fraction $\frac{7}{5}$ both equal the same amount. The whole number 3 and the improper fraction $\frac{12}{4}$ indicate the same amount.

Greater Than One

Working with Improper Fractions

An *improper fraction* always has a denominator smaller than or equal to the numerator. An improper fraction always indicates a value equal to or greater than one. The examples below are improper fractions.

$$\frac{3}{2}$$
 $\frac{9}{4}$ $\frac{6}{5}$ $\frac{9}{9}$ $\frac{1}{8}$

Directions: Read the Facts and Reminders page for this unit. Circle the improper fraction in each pair below.

1.
$$\frac{4}{3}$$
 $\frac{1}{4}$

2.
$$\frac{2}{8}$$
 $\frac{12}{11}$

3.
$$\frac{6}{5}$$

4.
$$\frac{9}{4}$$
 $\frac{1}{7}$

5.
$$\frac{7}{7}$$
 $\frac{1}{2}$

6.
$$\frac{7}{3}$$
 $\frac{7}{8}$

7.
$$\frac{4}{5}$$
 $\frac{6}{2}$

8.
$$\frac{8}{2}$$
 $\frac{5}{9}$

9.
$$\frac{10}{4}$$
 $\frac{3}{5}$

Directions: Study the Facts and Reminders page for this unit. Convert each of these improper fractions to a whole number. (*Remember:* Divide the denominator into the numerator to convert an improper fraction to a whole number.)

10.
$$\frac{8}{8}$$
 =

11.
$$\frac{15}{5}$$
 =

12.
$$\frac{14}{7}$$
 =

13.
$$\frac{35}{5}$$
 =

14.
$$\frac{6}{1}$$
 =

15.
$$\frac{8}{2}$$
 =

16.
$$\frac{3}{1}$$
 =

17.
$$\frac{25}{5}$$
 =

18.
$$\frac{22}{11}$$
 =

Directions: Circle the fraction with the highest value in each pair of improper fractions below.

19.
$$\frac{5}{5}$$
 $\frac{10}{5}$

20.
$$\frac{3}{3}$$
 $\frac{9}{3}$

21.
$$\frac{8}{2}$$
 $\frac{9}{3}$

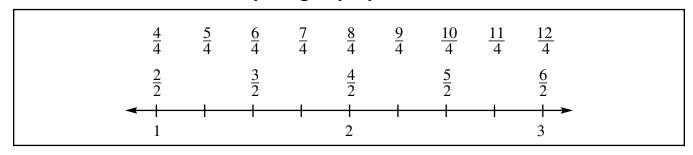
22.
$$\frac{5}{1}$$
 $\frac{4}{1}$

23.
$$\frac{6}{2}$$
 $\frac{12}{3}$

24.
$$\frac{8}{4}$$
 $\frac{8}{2}$

Greater Than One

Comparing Improper Fractions



Directions: Study the number line shown above. Circle the largest fraction in each pair listed below. Write an equal sign (=) if the fractions are equal to each other.

1.
$$\frac{3}{2}$$
 $\frac{5}{2}$

2.
$$\frac{4}{2}$$
 $\frac{8}{2}$

3.
$$\frac{6}{2}$$

4.
$$\frac{7}{4}$$
 $\frac{5}{2}$

5.
$$\frac{9}{4}$$
 $\frac{6}{2}$

6.
$$\frac{11}{4}$$
 $\frac{3}{2}$

7.
$$\frac{8}{4}$$
 $\frac{6}{2}$

8.
$$\frac{5}{2}$$
 $\frac{10}{4}$

9.
$$\frac{12}{4}$$

10.
$$\frac{6}{2}$$
 $\frac{12}{4}$

11.
$$\frac{3}{2}$$
 $\frac{6}{4}$

12.
$$\frac{11}{4}$$
 $\frac{5}{2}$

Directions: Change each improper fraction to a mixed number. Then illustrate each of the fractions as pies or pizzas. The first one is done for you.

13.
$$\frac{5}{4} = 1\frac{1}{4}$$

14.
$$\frac{3}{2}$$
 =

15.
$$\frac{7}{3}$$
 =





16.
$$\frac{8}{3}$$
 =

17.
$$\frac{9}{4}$$
 =

18.
$$\frac{7}{5}$$
 =

19.
$$\frac{7}{4}$$
 =

20.
$$\frac{5}{2}$$
 =

21.
$$\frac{12}{8}$$
 =

Greater Than One

Changing Improper Fractions to Mixed Numbers

An *improper fraction* always equals either a whole number or a mixed number. To convert an improper fraction into a whole number or mixed number, divide the denominator into the numerator. Write the quotient as a whole number and the remainder, if there is one, as a fraction.

$$\frac{7}{4}$$

$$\frac{1}{4)7}$$
 R 3

$$1\frac{3}{4}$$

Directions: Study the Facts and Reminders page for this unit. Change each of these improper fractions to a mixed number.

1.
$$\frac{9}{4}$$
 =

2.
$$\frac{9}{2}$$
 =

3.
$$\frac{10}{3}$$
 =

4.
$$\frac{8}{7} =$$

5.
$$\frac{12}{5}$$
 =

6.
$$\frac{13}{4}$$
 =

7.
$$\frac{10}{9}$$
 =

8.
$$\frac{4}{3}$$
 =

9.
$$\frac{7}{6}$$
 =

10.
$$\frac{14}{5}$$
 =

11.
$$\frac{7}{2}$$
 =

12.
$$\frac{15}{4}$$
 =

13.
$$\frac{19}{5}$$
 =

14.
$$\frac{9}{7}$$
 =

15.
$$\frac{15}{7}$$
 =

Sometimes the fraction part of a mixed number can be simplified or reduced, too. For example, $\frac{6}{4} = 1 \frac{2}{4} = 1 \frac{1}{2}$ (The $\frac{2}{4}$ can be simplified to $\frac{1}{2}$.)

Directions: Change these improper fractions to a mixed number. Simplify or reduce the fraction to lowest terms. The first one is done for you.

16.
$$\frac{8}{6} = 1\frac{2}{6} = 1\frac{1}{3}$$

17.
$$\frac{9}{6}$$
 =

18.
$$\frac{10}{4}$$
 =

19.
$$\frac{12}{8}$$
 =

20.
$$\frac{14}{4}$$
 =

21.
$$\frac{10}{8}$$
 =

22.
$$\frac{14}{10}$$
 =

23.
$$\frac{12}{9}$$
 =

24.
$$\frac{10}{6}$$
 =

25.
$$\frac{15}{10}$$
 =

Answer Key

Page 57		46		4,020; even	8. =
1. $D = RT$		78		10,472; even	9. 12/4
D = 50 x 5	7.	118	7.	43,824; even	10. =
D = 250 miles	8.	332	8.	21,616; even	11. =
2. $D = RT$	9.	104	9.	even	12. 11/4
D = 120 x 7	10.	28	10.	495; odd	13. 1 1/4
D = 840 miles	11.	78	11.	363; odd	14. 1 1/2
3. $D = RT$	12.	124	12.	9,513; odd	15. 2 1/3
$D = 9 \times 1.25$	13.	88	13.	9,139; odd	16. 2 2/3
D = 11.25 miles	14.	134		18,473; odd	17. 2 1/4
4. $D = RT$	15.	198		13,293; odd	18. 1 2/5
$D = 195 \times 3$	16.			11,439; odd	19. 1 3/4
D = 585 miles	17.			16,711; odd	20. 2 1/2
5. $D = RT$		296		odd	21. 1 1/2
$D = 7 \times 15.3$		even		8,584; even	
D = 107.1 miles		odd		30,774; even	Page 66
6. D = RT		even		19,762; even	1. 2 1/4
$D = 7 \times 12.3$		odd		3,696; even	2. 4 1/2
D = 86.1 miles		odd		even	3. 3 1/3
7. D = RT		even			4. 1 1/7
$D = 35.5 \times 11$		even	Page		5. 2 2/5
D = 390.5 miles		even		4/3	6. 3 1/4
D = 390.3 filles $8. D = RT$		even		12/11	7. 1 1/9
		110		6/5	8. 1 1/3
$D = 6.4 \times 5$				9/4	9. 1 1/6
D = 32 miles		100		7/7	10. 2 4/5
Page 58		Answers will vary.		7/3	11. 3 1/2
1. $T = D/R$	Page	61		6/2	12. 3 3/4
T = 1500/50	1.	592; even	8.	8/2	13. 3 4/5
T = 30 hrs.	2.	1,152; even	9.	10/4	14. 1 2/7
2. $T = D/R$	3.	4,020; even	10.	1	15. 2 1/7
T = 42/14	4.	9,676; even	11.	3	16. 1 1/3
T = 3 hrs.	5.	even	12.	2	17. 1 1/2
3. $T = D/R$	6.	428; even	13.	7	18. 2 1/2
T = 420/40	7.	428; even	14.	6	19. 1 1/2
T = 10.5 hrs.	8.	98; even	15.	4	20. 3 1/2
4. $T = D/R$	9.	6,404; even	16.	3	21. 1 1/4
T = 3250/50		even	17.	5	22. 1 2/5
T = 65 hrs.		16,604; even	18.		23. 1 1/3
5. $T = D/R$		8,094; even		10/5	24. 1 2/3
T = 44/5.5		11,324; even		9/3	25. 1 1/2
T = 8 hrs.		13,294; even		8/2	Page 68
6. T = D/R		even		5/1	_
T = 2980/40		2; even		12/3	1. 4 3/4
T = 74.5 hrs.		2,018; even		8/2	2. 9 5/6
7. $T = D/R$		118; even			3. 12 5/6
T = 2400/120		6,648; even	Page		4. 8 19/20
T = 2400/120 T = 20 hrs.		even		5/2	5. 12 9/10
				=	6. 10 7/8
Page 60	Page			6/2	7. 5 2/3
1. 8		752; even		5/2	8. 11 7/8
2. 24		384; even		6/2	9. 7 1/6
3. 14		4,440; even		11/4	10. 10 1/4
4. 38	4.	3,216; even	7.	6/2	11. 10 1/4